

# Subnanometer Displacements Measured by Fourier Transform Image Analysis

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**Christophe YAMAHATA,**  
**Edin SARAJLIC,**  
**Gijs J. M. KRIJNEN & Martin A. M. GIJS**

EPFL, STI, IMT • Laboratory of Microsystems

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# Outline

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## Theoretical background

→ Fourier transform applied to image analysis

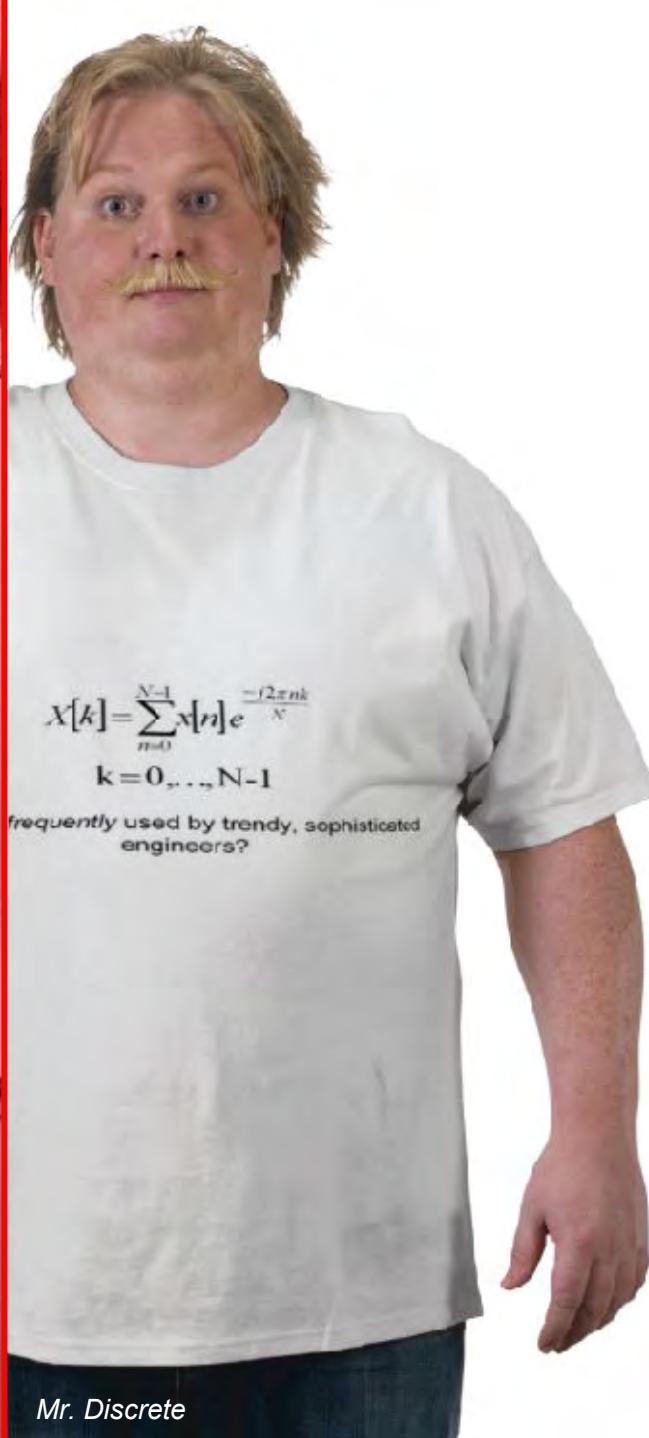
## Computing software

→ MATLAB Graphical User Interface

## Examples

- Movie scene with lots of gears
- Application to MicroElectroMechanical Systems (MEMS)

## Conclusion & Outlook



## Theoretical background

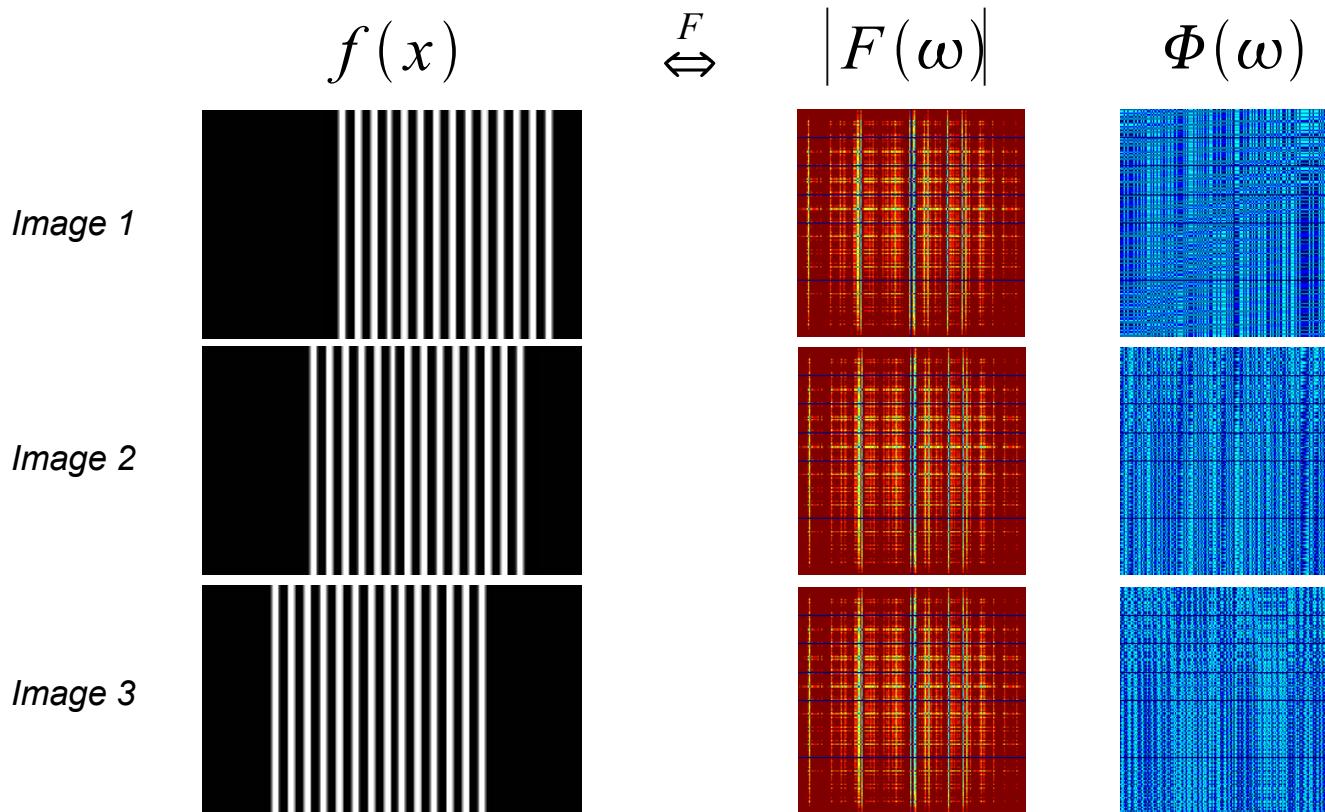
→ Fourier transform applied to image analysis

# Measurement method | Fourier transform image analysis

## Displacement measurement by Fourier transform analysis

The Fourier transform can be applied to **images** (2D function).

*Example: Fast Fourier Transforms of images*

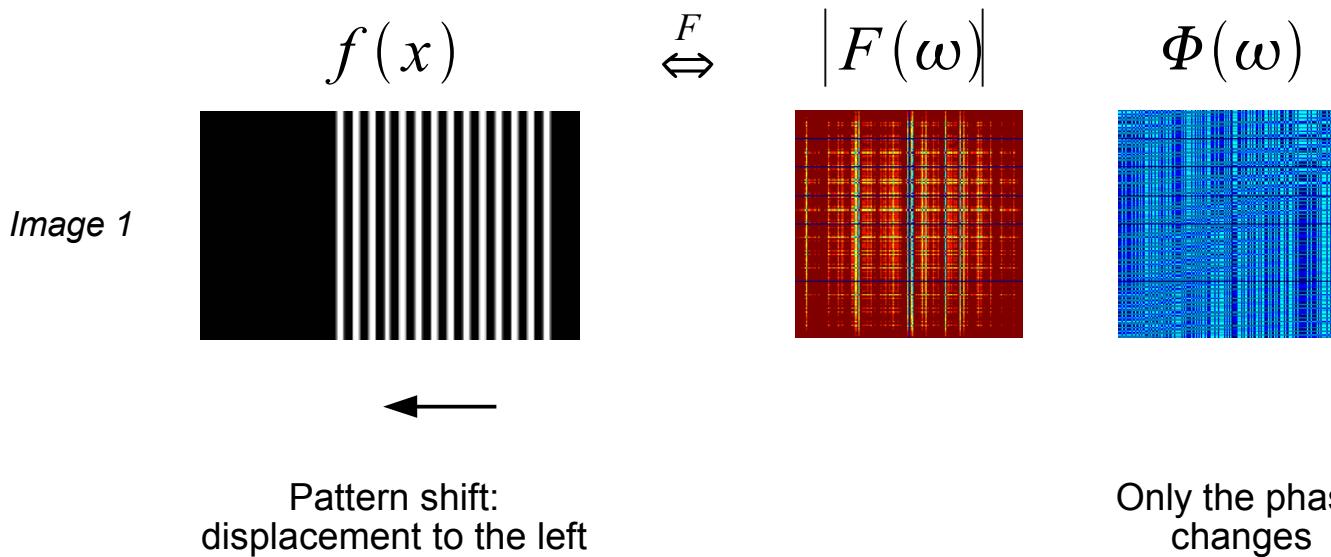


# Measurement method | Fourier transform image analysis

## Displacement measurement by Fourier transform analysis

The Fourier transform can be applied to **images** (2D function).

*Example: Fast Fourier Transforms of images*

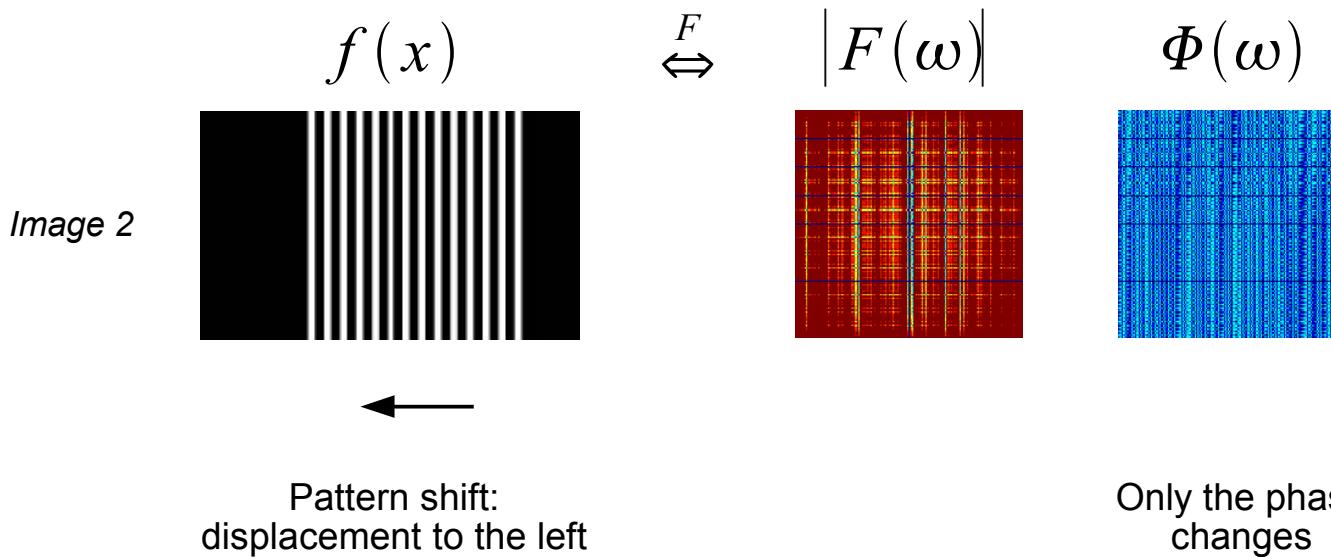


# Measurement method | Fourier transform image analysis

## Displacement measurement by Fourier transform analysis

The Fourier transform can be applied to **images** (2D function).

*Example: Fast Fourier Transforms of images*

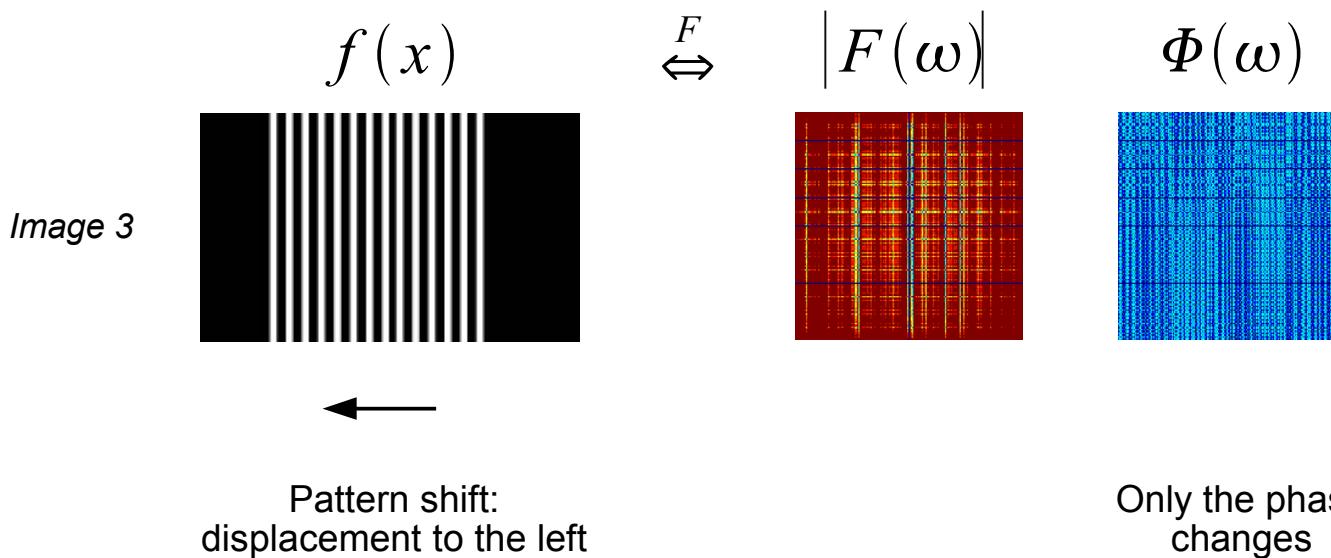


# Measurement method | Fourier transform image analysis

## Displacement measurement by Fourier transform analysis

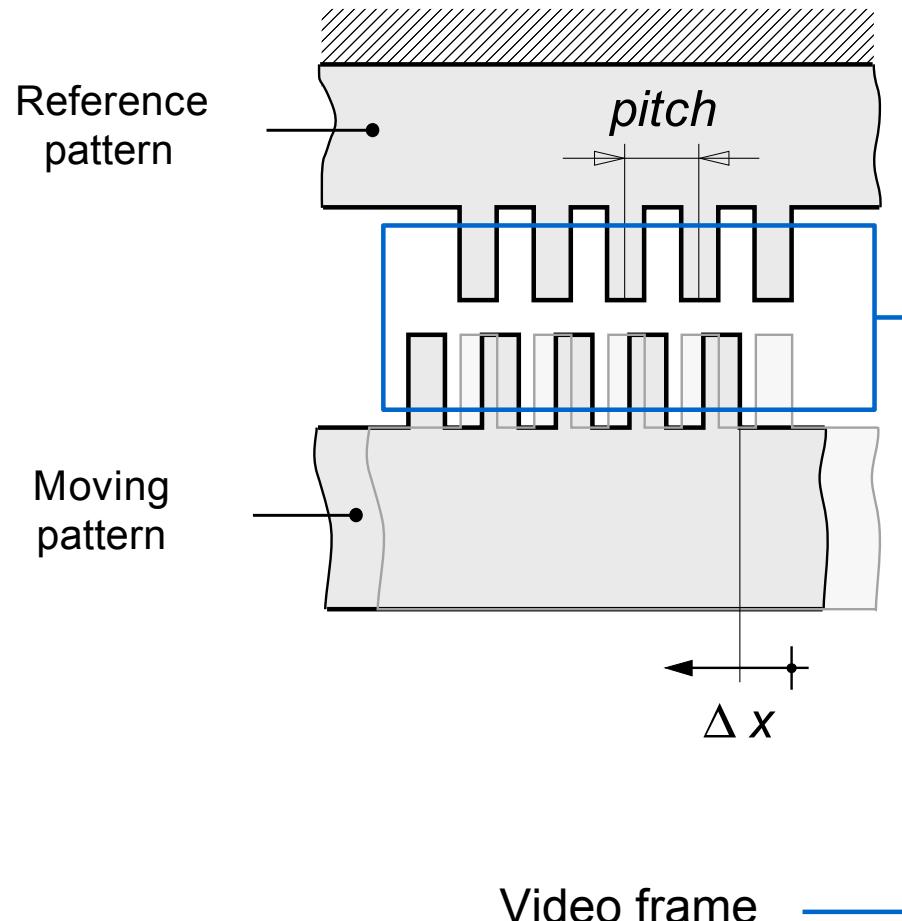
The Fourier transform can be applied to **images** (2D function).

*Example: Fast Fourier Transforms of images*



# Measurement method | Fourier transform image analysis

## Displacement measurement by Fourier transform analysis



Editor - D:\My documents (Yamahata)\FFT\_image\_analysis\_GUI\developers\FFT\_image\_

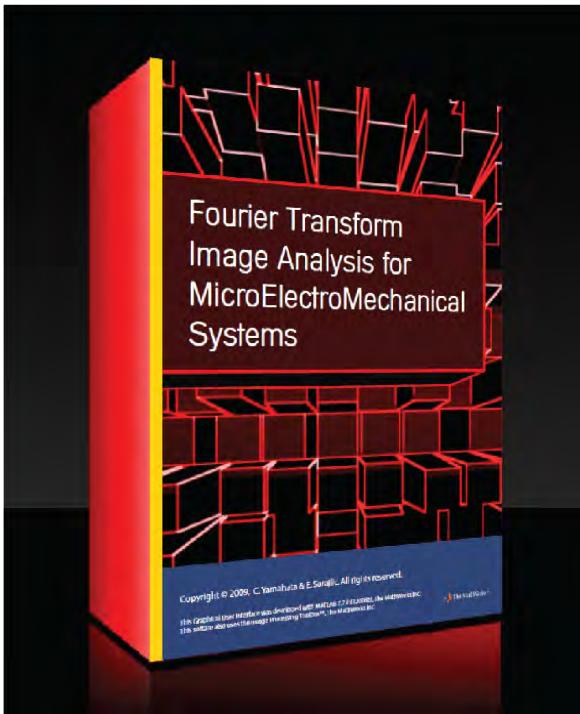
File Edit Text Go Cell Tools Debug Desktop Window Help

```
129 - set(handles.frame_v
130 - set(handles.slider_
131 % fr is the frame n
132 slider_pos = get(ha
133 avi_max_frame = fil
134 fr = max(1,round(sl
135
136 % load the frame fr
137 %img=aviread(file_1
138
139 % make a gray image
140 %img=rgb2gray(img.c
141 file_info = aviinfo(
142 if(strcmp(file_info
143 indexed_avi = a
144 [avi_frame,map]
145 img = ind2gray(
146 else
147 img = aviread(f
148 img = rgb2gray(
149 end
150
151 cla(handles.frame_v
152
153 colormap(handles.fr
154 image(img, 'Parent'
155
156
157 hold(handles.frame_
158 axis(handles.frame_
159 imshow(handles.frame
160
161
162 % --- Executes on b
163 function pushbutton
164 % hObject    handle to pushbutton (see GCBO)
165 % eventdata   reserved - to be defined by
166 % handles    struct containing handles and user data (see GUIDATA)
167
168 set(hObject,'Enable','inactive');
169 set(hObject,'ForegroundColor','red');
```

# Computing software

→ MATLAB Graphical User Interface (GUI)

# Computing software | MATLAB GUI



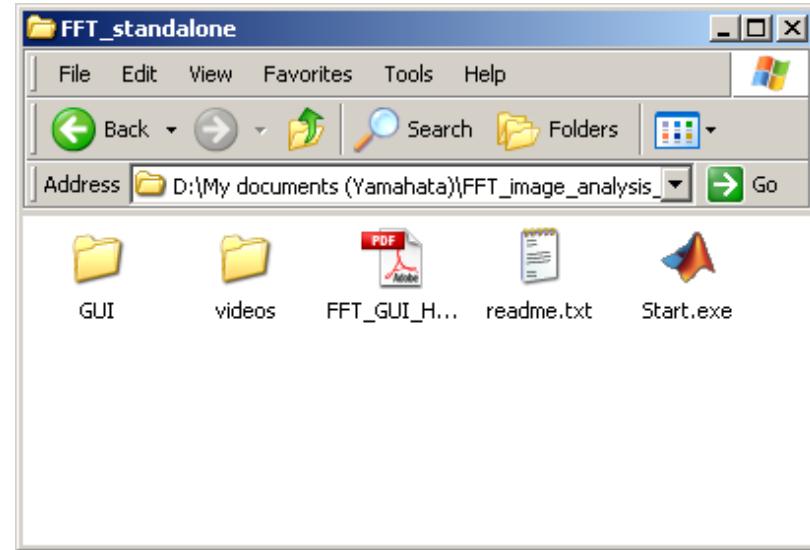
pcpq- ~O gvtqmi { 'hqt' O GO U



Available for download at

<http://lmis2.epfl.ch/nanoplus/>

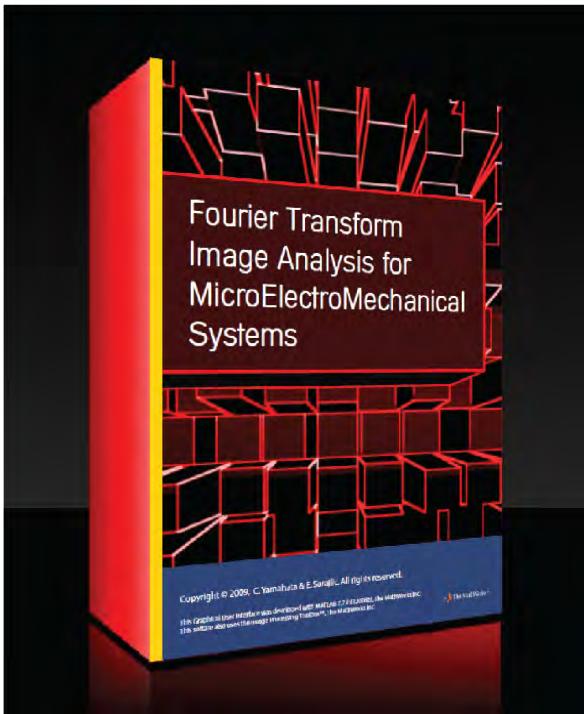
(free of charge)



The self-extracting package contains:

- MATLAB source files  
(" .m" script + ".fig" GUI)
- Standalone executable file (Windows)
- Sample videos
- Help document

# Computing software | MATLAB GUI



pcpq- ~O gvtqmi { 'hqt' O GO U



Available for download at

<http://lmis2.epfl.ch/nanoplus/>

(free of charge)

## Step 1: AVI selection

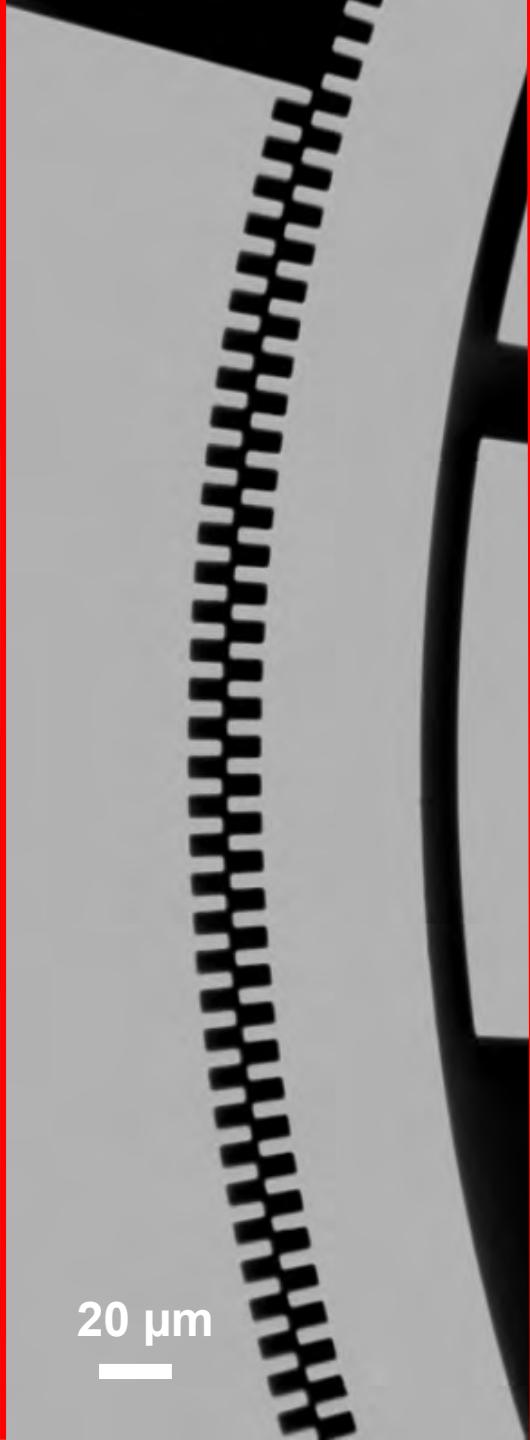
- Uncompressed **AVI file** ([recommended](#))
- AVI compressed with a MATLAB compatible compression codec:
  - Cinepak
  - Indeo3, Indeo5
  - MSVC (Microsoft Video 1)
  - 8-bit RLE, etc.

## Step 2: Area selection

- Select the **area of interest**
- Provide the **period** of the repeating patterns and the **width** of the video

## Step 3: Image analysis

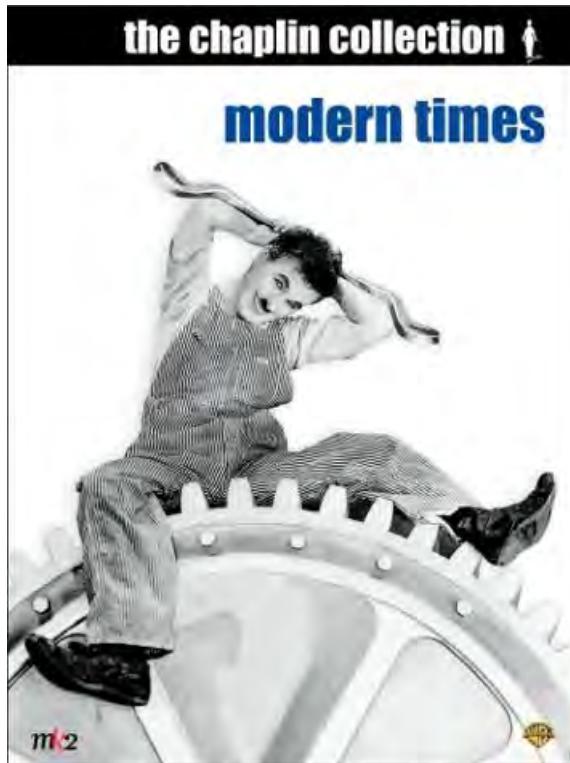
➔ Data can be **saved in Excel**



## Examples

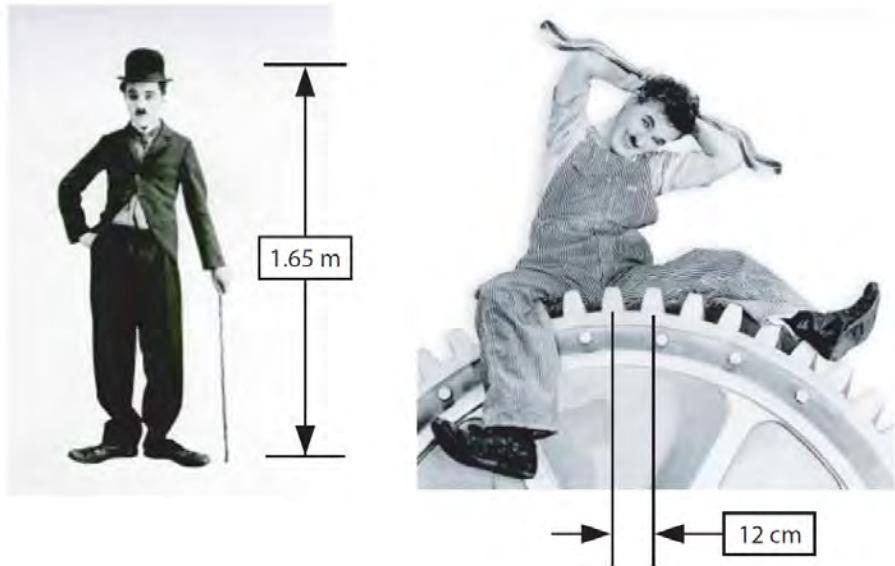
- Movie scene with lots of gears
- Application to MEMS

# Examples | Movie scene with lots of gears



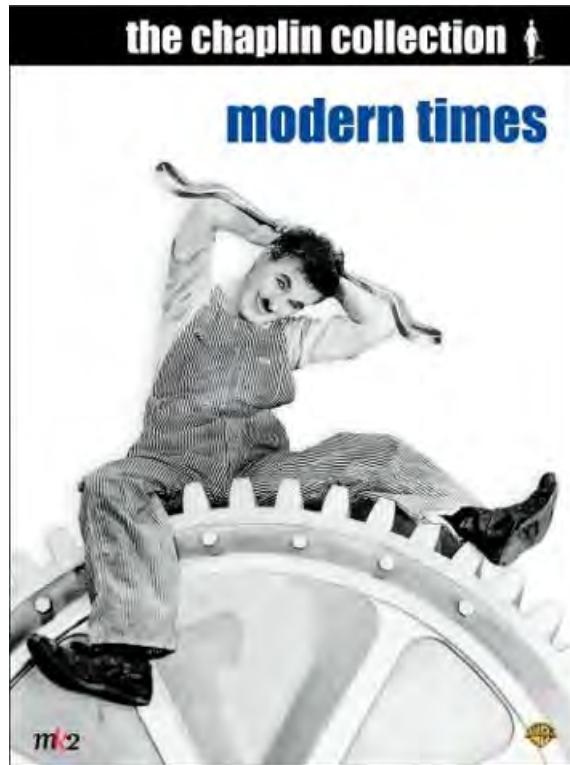
Trailer available online at  
<http://www.kino.com/moderntimes/>

## Parameters



→ The **period** of the repeating patterns, as well as the **width** of the video can be estimated (roughly).

# Examples | Movie scene with lots of gears



Trailer available online at  
<http://www.kino.com/moderntimes/>

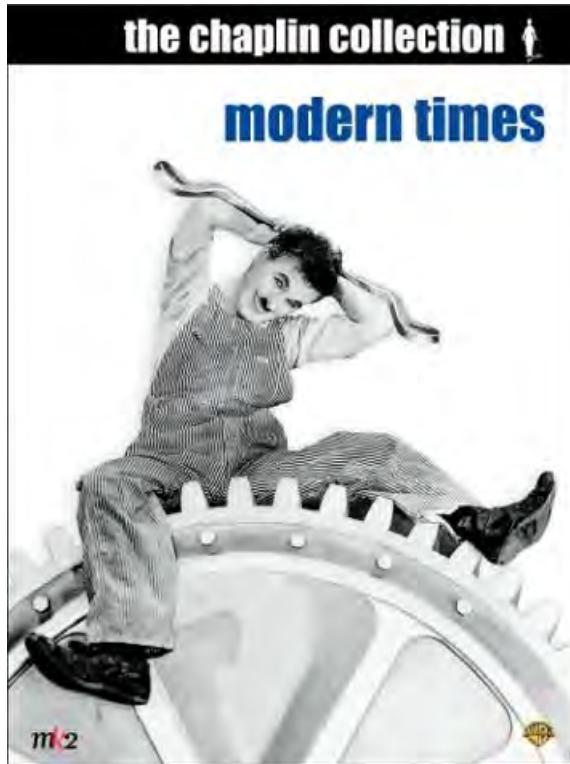
## Results

- Even though the **camera is moving** during the sequence, we can use the big gearing to estimate the displacement.

## Discussion

- **Camera position** must be:
  - Fixed
  - Perpendicular to the scene
- **Frame rate** must be high to avoid undersampling
  - Avoid aliasing
  - Eliminate wagon-wheel effect (Nyquist–Shannon sampling theorem)
- **Illumination** must be uniform (no shadowing)

# Examples | Movie scene with lots of gears

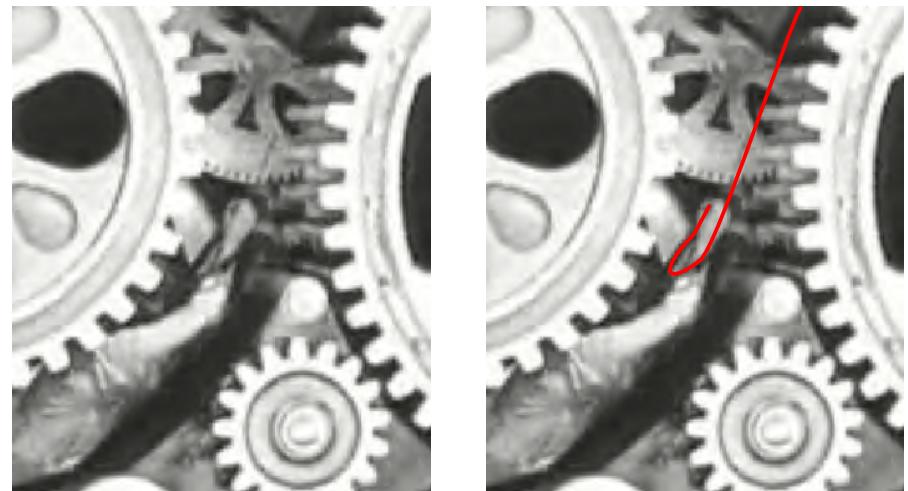


Trailer available online at  
<http://www.kino.com/moderntimes/>

## Results

- Even though the camera is moving during the sequence, we can use the big gearing to estimate the displacement.

Did you notice anything else?



# Examples | Application to MEMS

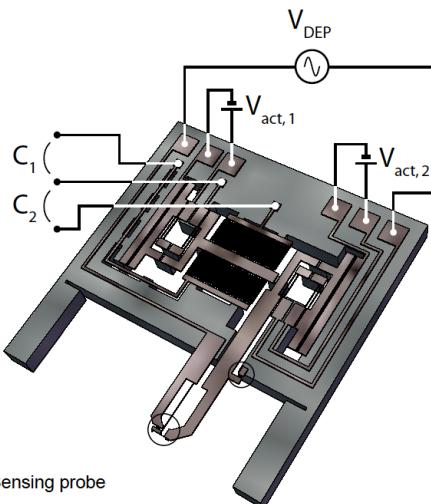
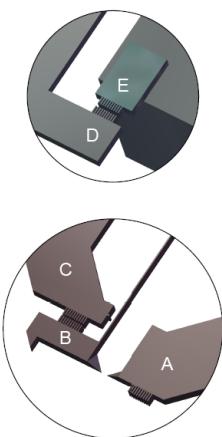
## Example 1: Calibration of a capacitive sensor

### Measurement method:

Spatial Fourier transform (imaging)  
+ Differential Capacitive Sensor

### FFT method:

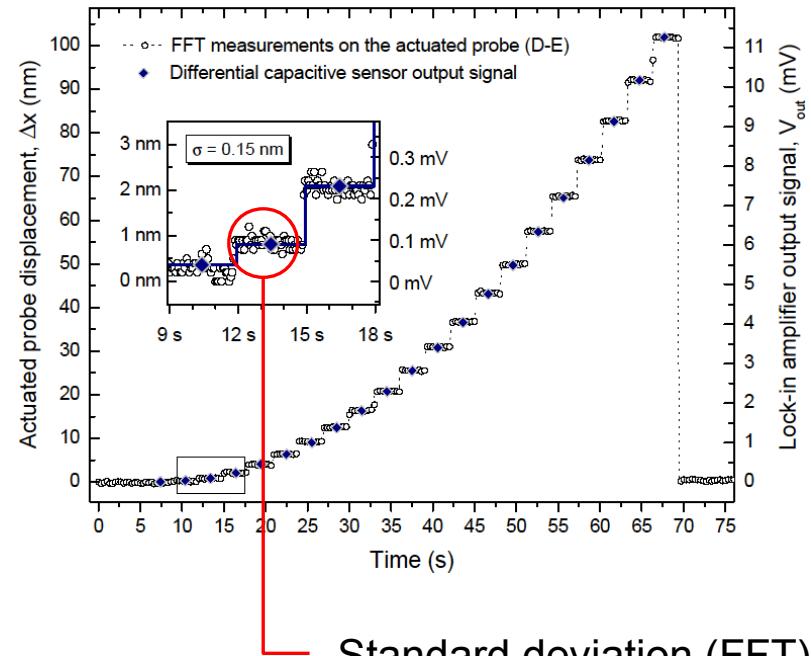
- Magnification  $\times 5000$
- AVI video  $800 \times 600$  pixels (15 fps)



A, D : Actuated probe  
C, E : Reference

B : Sensing probe

① Electrostatic actuation of the moving probe  
( $V_{act,1} = 0; 0.5 \text{ V}; 1 \text{ V}; \dots; 10 \text{ V}$ )



Standard deviation (FFT):  
 $\sigma = 0.15 \text{ nm}$

C. Yamahata, E. Sarajlic, L. Jalabert, M. Kumemura, D. Collard and H. Fujita

"Mechanical Characterization of Biomolecules in Liquid Using Silicon Tweezers with Subnanonewton Resolution,"  
Proc. 22<sup>nd</sup> IEEE Int. Conf. on Micro Electro Mechanical Systems (MEMS 2009), pp. 607-610, Sorrento, Italy, 2009.

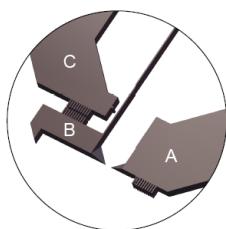
# Examples | Application to MEMS

## Example 2: Effect of vibrations

### Measurement method:

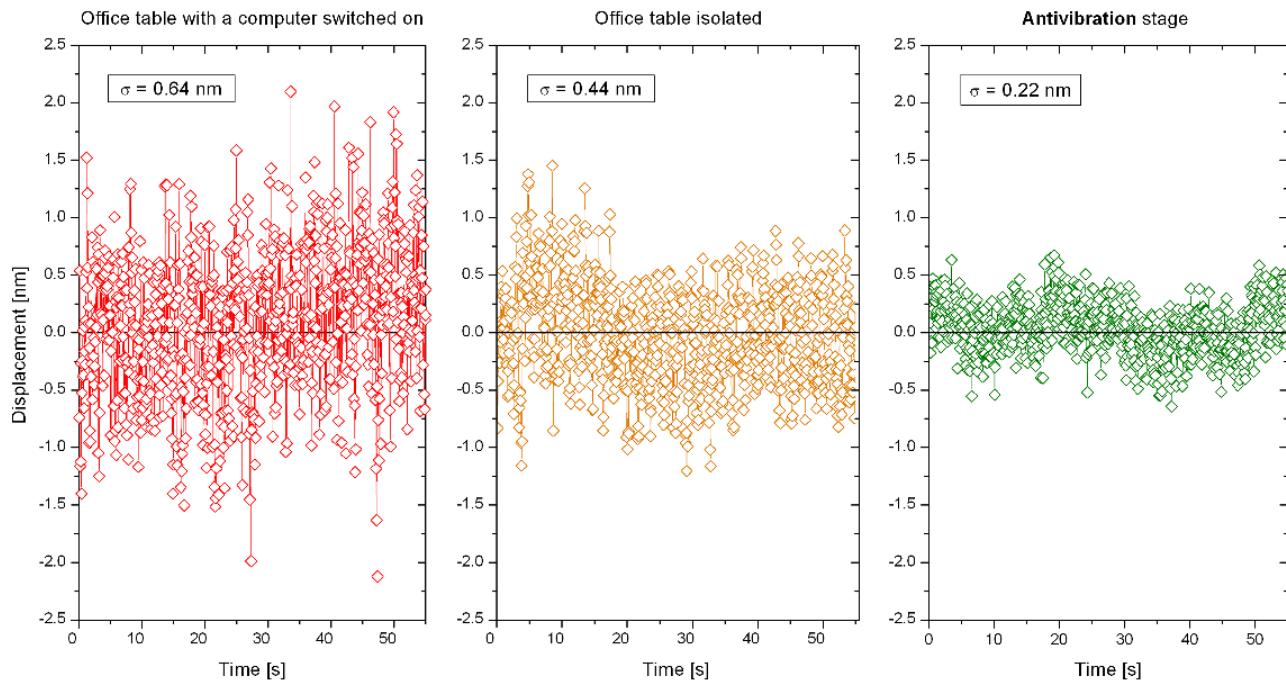
Spatial Fourier transform (imaging):

- Magnification  $\times 5000$
- AVI video **800  $\times$  600 pixels (15 fps)**



A, D : Actuated probe  
C, E : Reference

B : Sensing probe



# Examples | Application to MEMS

## Example 3: Displacement of a comb-drive actuator

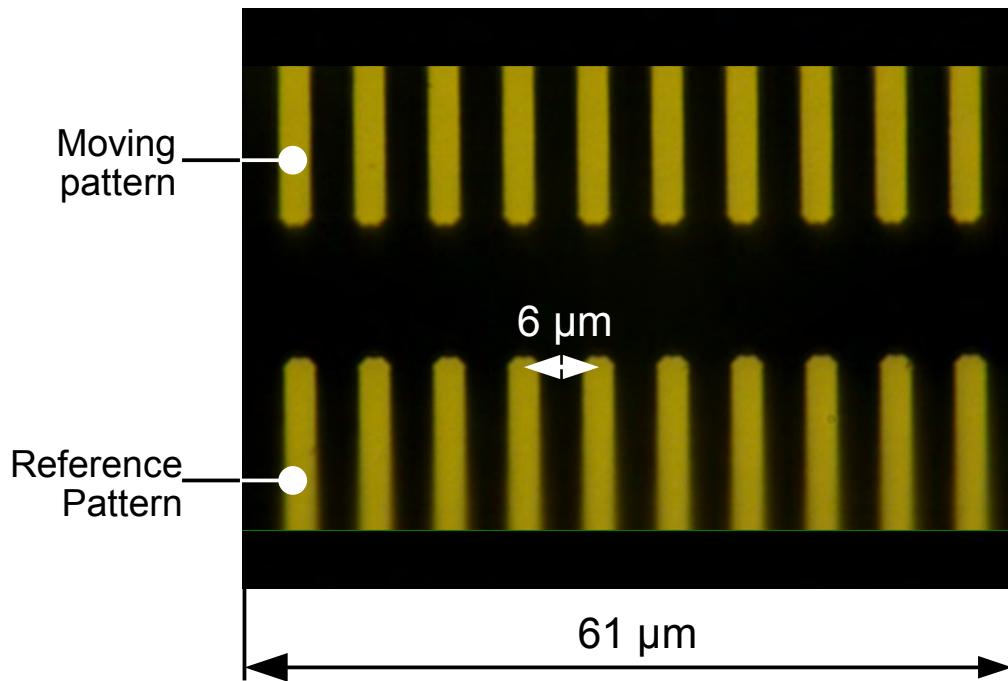
### Measurement method:

Spatial Fourier transform (imaging):

- Magnification  $\times 5000$
- AVI video  $800 \times 600$  pixels (15 fps)

#### Parameters:

- AVI width:  
**61 μm**
- Pattern period:  
**6 μm**



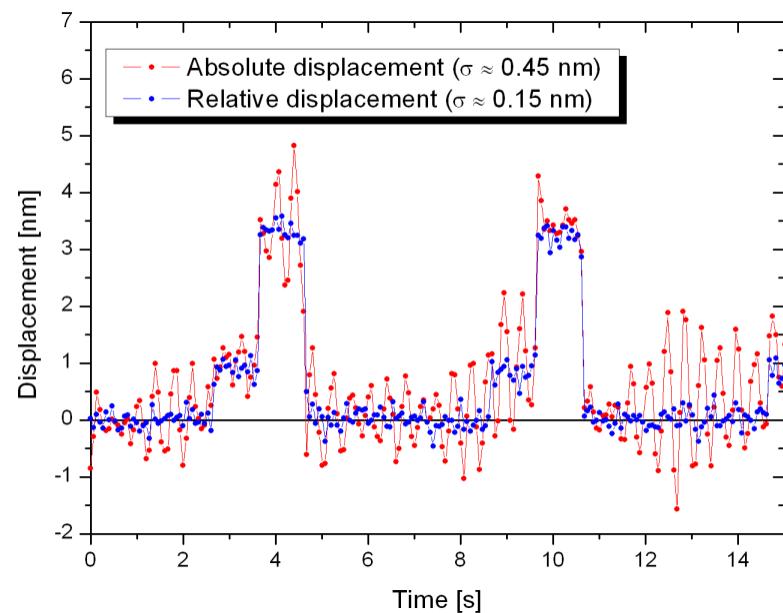
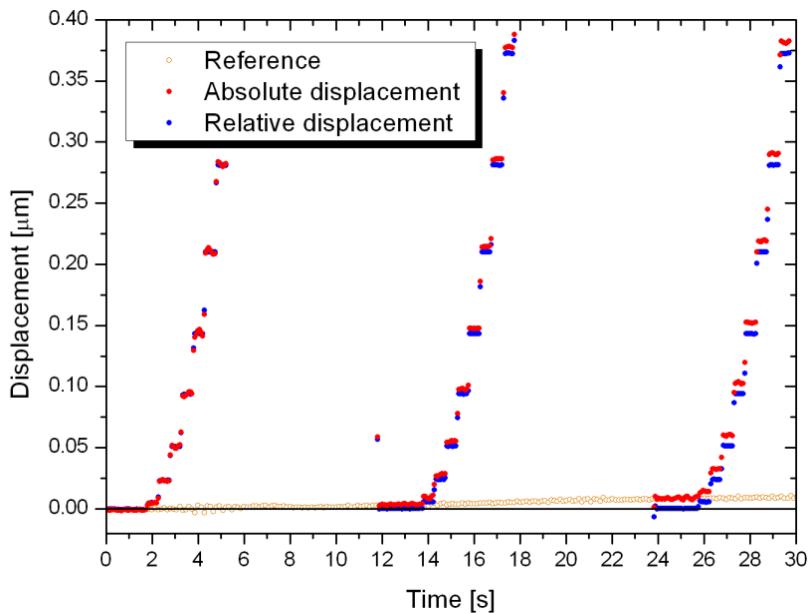
# Examples | Application to MEMS

## Example 3: Displacement of a comb-drive actuator

### Measurement method:

Spatial Fourier transform (imaging):

- Magnification  $\times 5000$
- AVI video **800  $\times$  600 pixels (15 fps)**





# Conclusion & outlook

# Conclusion & Outlook

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This method has been successfully used for the characterization of many types of MEMS devices.

- C. Yamahata *et al.*, “Mechanical characterization of biomolecules in liquid using silicon tweezers with subnanonewton resolution,” *Proc. IEEE MEMS*, pp. 607-610, Sorrento, Italy, January 25 – 29, 2009.
- E. Sarajlic *et al.*, “HAREM: High aspect ratio etching and metallization for microsystems fabrication,” *J. Micromech. Microeng.* **18** (7), 075008 (2008).
- E. Sarajlic *et al.*, “An electrostatic 3-phase linear stepper motor fabricated by vertical trench isolation technology,” *J. Micromech. Microeng.* **19** (7), 074001 (2009).
- and several other unpublished results ...

Many applications in the field of MEMS

- Easy to implement in any laboratory  
(digital camera attached to an optical microscope)
- Can be used to calibrate MEMS, perform strain/stress measurements at the micrometer scale, etc.